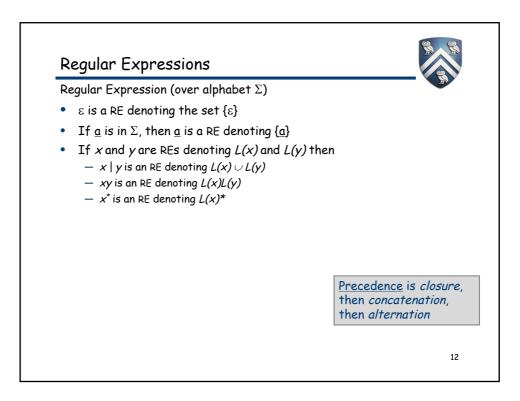


Operation	Definition
Union of L and M written L ∪ M	$L \cup M$ = { s s \in L or s \in M
Concatenation of L and M written LM	LM = { st $s \in$ L and t \in M]
Kleene closure of L written L*	L* = ∪ _{osis∞} Li
Positive closure of L written L⁺	L⁺ = ∪ _{1≤i≤∞} Li



Examples of Regular Expressions	
Identifiers: $Letter \rightarrow (\underline{a} \underline{b} \underline{c} \dots \underline{z} \underline{A} \underline{B} \underline{C} \dots \underline{Z})$ $Digit \rightarrow (\underline{0} \underline{1} \underline{2} \dots 9)$ $Identifier \rightarrow Letter (Letter Digit)^*$ $(\underline{a} \underline{b} \underline{c} \dots \underline{z} \underline{A} \underline{B} \underline{C} \dots \underline{Z}) (\underline{a} \underline{b} \underline{c} \dots \underline{z} \underline{A} \underline{B} \underline{C} $ Numbers:	shorthand for IZ) (0 1 2 19))*
$\begin{array}{rcl} Integer & \rightarrow (\underline{+} \underline{-} \epsilon) (\underline{0} (\underline{1} \underline{2} \underline{3} \dots \underline{9}) (Digit^*)) \\ Decimal & \rightarrow Integer \underline{.} \ Digit^* \\ Real & \rightarrow (Integer Decimal) \underline{E} (\underline{+} \underline{-} \epsilon) \ Digit \\ Complex \rightarrow (Real_Real) \end{array}$	*
Numbers can get much more complicated! Using symbolic names does not imply recursion	underlining indicates a letter in the input stream

